## Supporting Information

Temperature dependent amplified spontaneous emission in CsPbBr<sub>3</sub> thin films deposited by single-step RF-magnetron sputtering

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Figure S1: Absorption spectra of the two samples studied recorded at room temperature.



**Figure S2**: Comparison of the normalized emission spectra obtained at an excitation below and above threshold for both the samples studied, recorded at 50 K.



Figure S3: Complete dataset of the extracted thresholds in the samples studied, as a function of the temperature.



**Figure S4**: 3-level scheme, showing the main processes occurring during ASE action at different temperature ranges.



Figure S5: complete dataset of the PL intensities vs. temperature.



**Figure S6:** PL position and FWHM as a function of the temperature in both the samples S1 and S2, when excited at one half of the threshold density.

## Model of temperature dependence of ASE Thresholds in a 3-level system

If N is the whole population (volume density, cm<sup>-3</sup>) and  $n_0$  and  $n_1$  are the populations of the lower and upper states, respectively (with N =  $n_0+n_1$ ), the condition for population inversion is reached when a half of the carriers (N/2) occupies the upper state, i.e.  $n_1=N/2$ .

The amplification process starts when

$$\sigma(2n_1 - N) > \alpha \iff 2n_1 - N = \frac{\alpha}{\sigma} \tag{1}$$

where  $\alpha$  represents the losses coefficient and  $\sigma$  is the gain cross-section. Let  $n_{1th}$  be the population level at the threshold condition; the consequent depopulation rate at the threshold pumping can be expressed as

$$\frac{n_{1th}}{\tau} = \frac{1}{2} \left( \frac{\alpha}{\sigma} + N \right) \frac{1}{\tau} \tag{2}$$

Here,  $\frac{1}{\tau} = \frac{1}{\tau_0} + \frac{1}{\tau_{nr}}$  is the total decay rate at the threshold condition,  $\tau_0$  is the intrinsic transition lifetime and  $\tau_{nr}$  is the lifetime of a non-radiative process, a parameter accounting for eventual thermally activated processes, such as thermally induced carrier trapping/detrapping, exciton thermal dissociation, excitonexciton scattering, carrier thermal escape from the material, all of them detrimental for efficient ASE .<sup>[32]</sup> In fact, for a defined thermally induced non-radiative process (characterized by the lifetime  $\tau_T$  and an activation energy  $E_a$ ), the rate  $1/\tau_{nr}$  is expressed as

$$\frac{1}{\tau_{nr}} = \frac{1}{\tau_T} e^{-\frac{E_a}{kT}} \tag{3}$$

Where k is the Boltzmann constant.

In steady state regime (our pump pulse is much longer than the ASE lifetime) the excited state depopulation rate  $\frac{n_{1th}}{\tau}$  is equal to the excitation rate  $g_{0th}$ .

As the pump rate is directly proportional to the excitation density we finally have Dth=Cg0th and,

substituting Equation 3 in Equation 2 and compacting the temperature independent terms in  $D_0 =$ 

$$C\frac{1}{2}\left(\frac{\alpha}{\sigma}+N\right)\frac{1}{\tau_0}, D_1 = C\frac{1}{2}\left(\frac{\alpha}{\sigma}+N\right)\frac{1}{\tau_T}, \text{ and } D_{th} = C\frac{n_{2th}}{\tau}:$$
  
$$D_{th} = D_0 + D_1 e^{-\frac{E_a}{KT}}$$